Mathematics 1110H – Calculus I: Limits, Derivatives, and Integrals

TRENT UNIVERSITY, Winter 2021

Instructor

Department of Mathematics

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Prerequisite: Grade 12U Advanced Functions or equivalent with at least 60%. Strongly Recommended: Grade 12U Calculus and Vectors or equivalent.

Text

Single Variable Calculus (Early Transcendentals), by David Guichard, 2020, licensed under the Creative Commons BY-NC-SA License. May be downloaded for free from: communitycalculus.org

 $\mathbf{Meetings}$ – take the timetable with a grain of salt:

Lectures will be pre-recorded and posted to Blackboard, usually on Monday, Wednesday, and Friday mornings. Though it is unlikely, the lecture times given in the timetable may be used for other purposes, if necessary, such as additional office hours.

Seminars will occur at the times given in the timetable (Fridays 09:00-09:50) via Zoom and will focus on answering questions about the material, the quizzes, and the assignments. (Seminars will not be recorded.) Labs will occur at the times given in the timetable (Mondays 19:00-19:50) via Zoom and will focus on Maple and on tutoring: helping with developing necessary skills, homework exercises, and the like. (Labs will not be recorded.)

Marking Scheme

There will be eleven weekly quizzes (which will be 24-hour mini-assignments), at least six fortnightly assignments, and a three-day take-home final examination, counted so:

| Best 10 quizzes (3.5% each) | 35% |
|------------------------------|-----|
| Best 5 assignments (6% each) | 30% |
| Final examination | 35% |

Please note that work worth at least 25% of the course should be completed, marked, and returned by the final date (Monday, 15 March) to withdraw from the course without academic penalty. Students who miss more than one quiz or assignment for reasons beyond their control should contact the instructor as soon as possible to arrange to write a make-up. Quizzes and assignments will be accepted after they are due at the instructor's sole discretion.

This scheme may be modified for individual students in *exceptional* circumstances, such as a lengthy absence due to illness. Any such modification will require the agreement of both the student and the instructor.

Content and Learning Outcomes

MATH 1110H is an introduction to the concepts and techniques of differential and some integral singlevariable calculus, with some applications to other areas of mathematics and science. Upon successful completion of this course, a student should be able to:

- 1. Compute limits of functions, using both direct (e.g. algebraic) and indirect (e.g. squeeze-play) methods.
- 2. Determine where and whether functions are continuous, and identify and classify points of discontinuity.
- 3. Differentiate a wide class of single-variable functions, including polynomials, algebraic functions, trigonometric functions, exponential and logarithmic functions, and sums, products, quotients, compositions, and inverses of these functions. Integrate such functions using methods up to and including substitution.
- 4. Use the first and second derivatives and asymptotics of a function to obtain qualitative information about that function, such as intervals of increase or decrease, concavity, maxima and minima, existence and uniqueness of roots. Use this information to sketch the graph of the function.
- 5. Use derivatives to solve applied problems involving rate-of-change, linear approximation, and optimization. Understand the meaning of core calculus concepts in simple applications to physics, engineering, economics, biology, and other sciences.
- 6. Use integration to compute areas under curves and the volumes of rotationally symmetric solids.
- 7. Have sufficient abstract conceptual understanding of continuity, derivatives, integrals, and antiderivatives to can understand the main ideas in the proofs of some of the classical results of calculus (*e.g.* the Mean Value and Squeeze Theorems) and understand and use the statements of others (*e.g.* the Fundamental Theorem of Calculus).

Schedule

In terms of content, this schedule should be taken with a grain of salt: no lesson plan survives contact with students unchanged. We will speed up or slow down, and perhaps rearrange some material, depending on how things go. Please note that while we will not fully cover the content of every chapter, we will from time to time cover bits of material that are not in the textbook. Note also that a number of the assignments will involve using Maple or similar software to plot functions and solve calculus problems.

Weeks 1–2. (11-22 January) Classes begin on Monday, 11 January. Chapters 1–2: Functions, limits, continuity, definition of the derivative. Quiz #1 written on Tuesday, 19 January; Assignment #1 due on Friday, 22 January.

Weeks 3–4. (25 January – 5 February) Chapters 3–4: Derivatives, curve sketching, Product, Quotient, and Chain Rules, trigonometric functions. Quiz #2 written on Tuesday, 26 January; Quiz #3 written on Tuesday, 2 February; Assignment #2 due on Friday, 5 February.

Weeks 5–6. (8-12 & 22-26 February) Chapters 4–5: Exponential, logarithmic, and hyperbolic functions, curve sketching. Quiz # 4 written on Tuesday, 9 February; Quiz #5 written on Tuesday, 16 February; Assignment #3 due on Friday, 19 February.

Catch-up Reading Week. (15-19 February) Between Weeks 5 & 6. Enjoy!

Weeks 7–8. (1-12 March) Chapter 6: applications of differentiation, optimization. Quiz #6 written on Tuesday, 2 March; Quiz #7 written on Tuesday, 9 March; Assignment #4 due on Friday, 12 March.

Weeks 9–10. (15-26 March) Chapters 7–8: Integrals, the Fundamental Theorem of Calculus, techniques of integration. The last day to withdraw from Winter courses is Monday, 15 March. Quiz #8 written on Tuesday, 16 March; Quiz #9 written on Tuesday, 23 March; Assignment #5 due on Friday, 26 March.

Weeks 11–12. (29 March – 9 April) Chapters 8–9: Techniques of integration, applications of integration. Quiz #10 written on Tuesday, 30 March; Quiz #11 written on Tuesday, 6 April; Assignment #6 due on Friday, 9 April. Friday, 9 April, is the last day of classes.

Winter Examination Period. (12-23 April) Exam schedule to be announced. The take-home exam will be written over three days during the winter examination period, probably 14-16 April.

Academic Integrity

Academic dishonesty, which includes plagiarism and cheating, is an extremely serious academic offence and carries penalties varying from a 0 grade on an assignment to expulsion from the University. Definitions, penalties, and procedures for dealing with plagiarism and cheating are set out in Trent University's Academic Integrity Policy. You have a responsibility to educate yourself – unfamiliarity with the policy is not an excuse. You are strongly encouraged to visit Trent's Academic Integrity website to learn more – www.trentu.ca/academicintegrity

For clarity, the following guidelines will apply in MATH 1110H:

You are permitted and encouraged to work with others and ask anyone willing (especially the instructor!) for explanations, hints, and suggestions on the assignments, and to consult whatever sources you wish. However, all work submitted for credit must be written up entirely by yourself, giving due credit to all relevant sources of help and information. For the quizzes and final exam, you may not give or receive any help, nor use any aids except for a calculator (any that you like) and the materials from this course (textbook, all handouts, lectures, your own notes, *etc.*), except with the instructor's express permission.

Access to Instruction

It is Trent University's intent to create an inclusive learning environment. If a student has a disability and/or health consideration and feels that he/she may need accommodations to succeed in this course, the student should contact the Student Accessibility Services Office (SAS), Blackburn Hall Suite 132, 705 748-1281, sas@trentu.ca. For Trent University in Oshawa Student Accessibility Services Office contact 905 435-5102, ext. 5024. Complete text can be found under Access to Instruction in the Academic Calendar.

Blackboard and Web Archive Page

All course materials will be posted to or linked from the course Blackboard site. A web page at euclid.trentu.ca/math/sb/1110H/ will archive this material, as well as material from a number of previous iterations of first-year calculus.

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