TRENT UNIVERSITY, WINTER 2020 MATH 1120H Test Thursday, 27 February Time: 50 minutes

Instructions

- Show all your work. Legibly, please! Simplify where you reasonably can.
- If you have a question, ask it!
- Use the back sides of all the pages for rough work or extra space.
- You may use a calculator and (all sides of) an aid sheet.
- **1.** Compute any four (4) of integrals **a**–**f**. $[12 = 4 \times 3 \text{ each}]$

a.
$$\int \frac{1}{1-t^2} dt$$
 b. $\int_0^1 \arctan(x) dx$ **c.** $\int \frac{z^2}{z^3+z} dz$
d. $\int_0^\infty y e^{-y^2} dy$ **e.** $\int \cos^3(w) dw$ **f.** $\int_0^1 \sqrt{1-r^2} dr$

- **2.** Do any two (2) of parts $\mathbf{a}-\mathbf{c}$. $[10 = 2 \times 5 \text{ each}]$
- **a.** Find the area of the finite region below y = 2 x and above $y = x^2$.
- **b.** Find the area of the surface obtained by revolving the curve y = x, for $0 \le x \le 4$, about the *y*-axis.
- c. Find the volume of the solid obtained by revolving the region between $y = \sqrt{x}$ and y = 0, where $0 \le x \le 4$, about the x-axis.
- **3.** Do either one (1) of parts \mathbf{a} or \mathbf{b} . [8]

a. Find the arc-length of the curve
$$y = \frac{1}{4}x^2 - \frac{1}{2}\ln(x)$$
, where $1 \le x \le 2e$.

b. Compute $\int \frac{\cos(x)}{\sin^3(x) + \sin(x)} dx.$

0

[Total = 30]