## Trent University, Winter 2020

MATH 1120H Test
Thursday, 27 February
Time: 50 minutes

## Instructions

- Show all your work. Legibly, please! Simplify where you reasonably can.
- If you have a question, ask it!
- Use the back sides of all the pages for rough work or extra space.
- You may use a calculator and (all sides of) an aid sheet.

1. Compute any four (4) of integrals a-f. $[12=4 \times 3$ each $]$
a. $\int \frac{1}{1-t^{2}} d t$
b. $\int_{0}^{1} \arctan (x) d x$
c. $\int \frac{z^{2}}{z^{3}+z} d z$
d. $\int_{0}^{\infty} y e^{-y^{2}} d y$
e. $\int \cos ^{3}(w) d w$
f. $\int_{0}^{1} \sqrt{1-r^{2}} d r$
2. Do any two (2) of parts a-c. [10 $=2 \times 5$ each]
a. Find the area of the finite region below $y=2-x$ and above $y=x^{2}$.
b. Find the area of the surface obtained by revolving the curve $y=x$, for $0 \leq x \leq 4$, about the $y$-axis.
c. Find the volume of the solid obtained by revolving the region between $y=\sqrt{x}$ and $y=0$, where $0 \leq x \leq 4$, about the $x$-axis.
3. Do either one (1) of parts a or b. [8]
a. Find the arc-length of the curve $y=\frac{1}{4} x^{2}-\frac{1}{2} \ln (x)$, where $1 \leq x \leq 2 e$.
b. Compute $\int \frac{\cos (x)}{\sin ^{3}(x)+\sin (x)} d x$.
