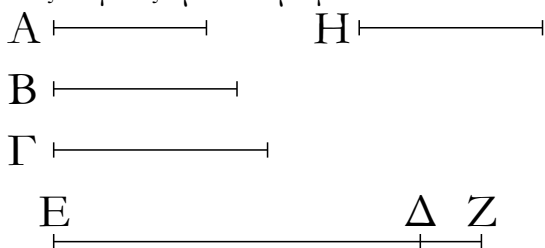


κ΄.

Οἱ πρῶτοι ἀριθμοὶ πλείους εἰσὶ παντὸς τοῦ προ-
τεθέντος πλήθους πρῶτων ἀριθμῶν.



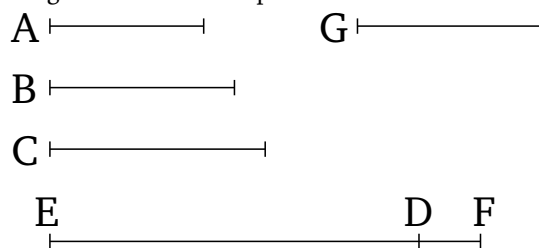
Ἐστῶσαν οἱ προτεθέντες πρῶτοι ἀριθμοὶ οἱ A, B, Γ . λέγω, ὅτι τῶν A, B, Γ πλείους εἰσὶ πρῶτοι ἀριθμοί.

Εἰλήφθω γὰρ ὁ ὑπὸ τῶν A, B, Γ ἐλάχιστος με-
τρούμενος καὶ ἔστω ΔE , καὶ προσκείσθω τῷ ΔE μονὰς
ἢ ΔZ . ὁ δὲ EZ ἤτοι πρῶτός ἐστιν ἢ οὐ. ἔστω πρότερον
πρῶτος· εὐρημένοι ἄρα εἰσὶ πρῶτοι ἀριθμοὶ οἱ $A, B, \Gamma, \Gamma,$
 EZ πλείους τῶν A, B, Γ .

Ἄλλὰ δὴ μὴ ἔστω ὁ EZ πρῶτος· ὑπὸ πρώτου ἄρα
τινὸς ἀριθμοῦ μετρεῖται. μετρεῖσθω ὑπὸ πρώτου τοῦ H .
λέγω, ὅτι ὁ H οὐδενὶ τῶν A, B, Γ ἐστὶν ὁ αὐτός. εἰ γὰρ
δυνατὸν, ἔστω. οἱ δὲ A, B, Γ τὸν ΔE μετροῦσιν· καὶ
ὁ H ἄρα τὸν ΔE μετρήσει. μετρεῖ δὲ καὶ τὸν EZ · καὶ
λοιπὴν τὴν ΔZ μονάδα μετρήσει ὁ H ἀριθμὸς ὧν ὅπερ
ἄτοπον. οὐκ ἄρα ὁ H ἐνὶ τῶν A, B, Γ ἐστὶν ὁ αὐτός. καὶ
ὑπόκειται πρῶτος. εὐρημένοι ἄρα εἰσὶ πρῶτοι ἀριθμοὶ
πλείους τοῦ προτεθέντος πλήθους τῶν A, B, Γ οἱ $A, B,$
 Γ, H · ὅπερ ἔδει δεῖξαι.

Proposition 20

The (set of all) prime numbers is more numerous than
any assigned multitude of prime numbers.



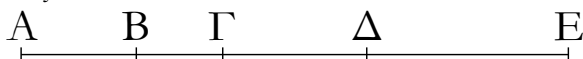
Let A, B, C be the assigned prime numbers. I say that
the (set of all) primes numbers is more numerous than $A,$
 B, C .

For let the least number measured by A, B, C have
been taken, and let it be DE [Prop. 7.36]. And let the
unit DF have been added to DE . So EF is either prime
or not. Let it, first of all, be prime. Thus, the (set of)
prime numbers A, B, C, EF , (which is) more numerous
than A, B, C , has been found.

And so let EF not be prime. Thus, it is measured by
some prime number [Prop. 7.31]. Let it be measured by
the prime (number) G . I say that G is not the same as
any of A, B, C . For, if possible, let it be (the same). And
 A, B, C (all) measure DE . Thus, G will also measure
 DE . And it also measures EF . (So) G will also mea-
sure the remainder, unit DF , (despite) being a number
[Prop. 7.28]. The very thing (is) absurd. Thus, G is not
the same as one of A, B, C . And it was assumed (to be)
prime. Thus, the (set of) prime numbers $A, B, C, G,$
(which is) more numerous than the assigned multitude
(of prime numbers), A, B, C , has been found. (Which is)
the very thing it was required to show.

κα΄.

Ἐὰν ἄρτιοι ἀριθμοὶ ὅποσοιῶν συντεθῶσιν, ὁ ὅλος
ἄρτιός ἐστιν.

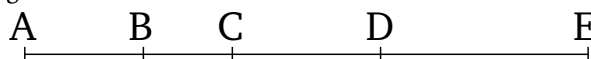


Συγκείσθωσαν γὰρ ἄρτιοι ἀριθμοὶ ὅποσοιῶν οἱ $AB,$
 $B\Gamma, \Gamma\Delta, \Delta E$. λέγω, ὅτι ὅλος ὁ AE ἄρτιός ἐστιν.

Ἐπεὶ γὰρ ἕκαστος τῶν $AB, B\Gamma, \Gamma\Delta, \Delta E$ ἄρτιός ἐστιν,
ἔχει μέρος ἡμισυ· ὥστε καὶ ὅλος ὁ AE ἔχει μέρος ἡμισυ.
ἄρτιος δὲ ἀριθμὸς ἐστὶν ὁ δίχα διαιρούμενος· ἄρτιος
ἄρα ἐστὶν ὁ AE · ὅπερ ἔδει δεῖξαι.

Proposition 21

If any multitude whatsoever of even numbers is added
together then the whole is even.



For let any multitude whatsoever of even numbers,
 AB, BC, CD, DE , lie together. I say that the whole,
 AE , is even.

For since everyone of AB, BC, CD, DE is even, it
has a half part [Def. 7.6]. And hence the whole AE has
a half part. And an even number is one (which can be)
divided in two [Def. 7.6]. Thus, AE is even. (Which is)
the very thing it was required to show.