

Prop: Suppose  $f(z) = \sum_{n=0}^{\infty} c_n (z-a)^n$  has radius of convergence  $R > 0$ . Then  $c_n = \frac{f^{(n)}(a)}{n!}$  for all  $n \geq 0$ . (3)

[This is Taylor's formula.]

proof:  $f(a) = c_0 \Rightarrow c_0 = \frac{f^{(0)}(a)}{0!}$  as  $0! = 1$

$f'(a) = f^{(1)}(a) = 1 \cdot c_1 \Rightarrow c_1 = \frac{f^{(1)}(a)}{1!}$  as  $1! = 1$

⋮

Corollary: If  $\sum_{n=0}^{\infty} c_n (z-a)^n$  &  $\sum_{n=0}^{\infty} d_n (z-a)^n$  both converge to the same function on some open disk centred at  $a$ , then  $c_n = d_n$  for all  $n$ . //