

## Power Series: Taylor Series

Corollary to previous results:

Suppose  $\sum_{n=0}^{\infty} c_n (z-a)^n$  has radius of convergence  $R$ ,

and  $\gamma$  is a (piecewise smooth) path in the disk

$D = \{z \mid |z-a| < R\}$ . Then

$$\int_{\gamma} \left( \sum_{n=0}^{\infty} c_n (z-a)^n \right) dz = \sum_{n=0}^{\infty} \left( \int_{\gamma} c_n (z-a)^n dz \right).$$

Note that it follows that if  $\gamma$  is closed,

then  $\int_{\gamma} \left( \sum_{n=0}^{\infty} c_n (z-a)^n \right) dz = 0$ .

Thm: Suppose  $f(z) = \sum_{n=0}^{\infty} c_n (z-a)^n$  has radius of convergence  $R > 0$ . Then  $f(z)$  is holomorphic in the (open) disk  $D = \{z \mid |z-a| < R\}$ .