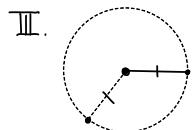


"Neutral" Geometry

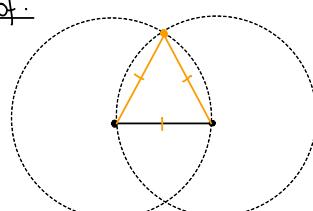
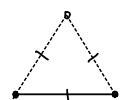
What can we do (with triangles especially) without Post. IV?

I. 
II. 

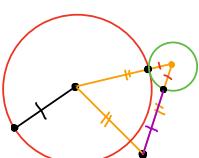
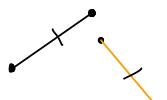


IV. $b = b$

Prop. I-1:  Proof:

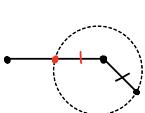


I-2:  Proof:

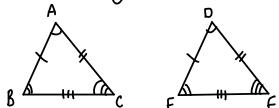


I-3:

Proof:



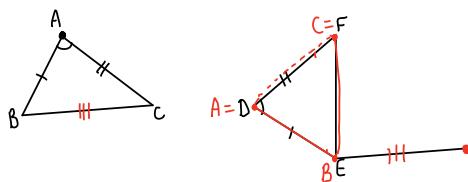
I-4: SAS Congruence Criterion



Proof:

Suppose $\triangle ABC$ and $\triangle DEF$ have $\angle A = \angle D$, $AB = DE$ and $AC = DF$.

To Show: $BC = EF$, $\angle B = \angle E$, and $\angle C = \angle F$



• "Apply" $\triangle ABC$ to $\triangle DEF$ so that A falls on D,
AB falls along DE,

& C ends up on the same side of DE as F does

• $AB = DE$ and since A is on D and AB is along DE, B falls on E

• Since $\angle A = \angle D$ and AB is along DE and C is on the same side of F, AC falls along DF

• Since $AC = DF$ it also follows that C falls on F

• But then $BC = EF$.

& $\angle B = \angle E$

& $\angle C = \angle F$.