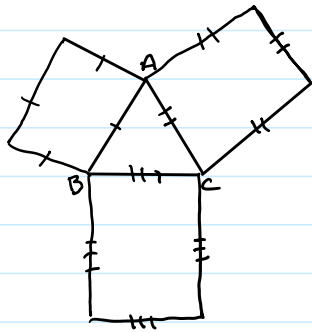
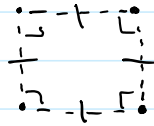


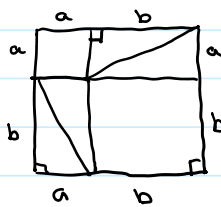
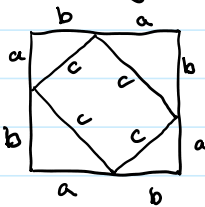
Lecture 14

Saturday, February 10, 2024 10:40 AM

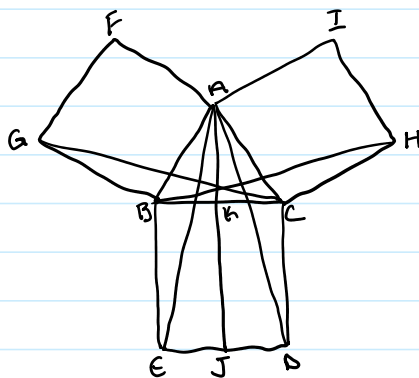
I-46: Given a line segment, construct a square on it.



I-47: (pythagorean Theorem) $a^2 + b^2 = c^2$



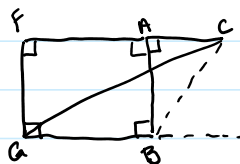
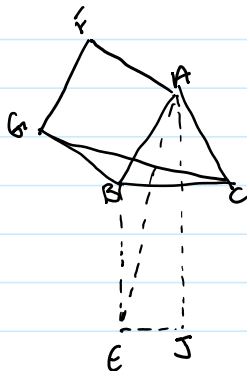
$$\therefore a^2 + b^2 = c^2$$



Proof: **Step 1:** $\angle GBC = \angle ABE$
 (both are $90^\circ + \angle ABC$) and $\angle ACD = \angle HCB$
 (both are $90^\circ + \angle ACB$)

Step 2: (S-A-S \cong)
 $\triangle GBC \cong \triangle ABE$ and $\triangle ACD \cong \triangle HCB$

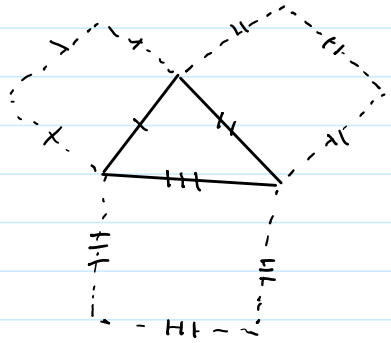
Step 3:



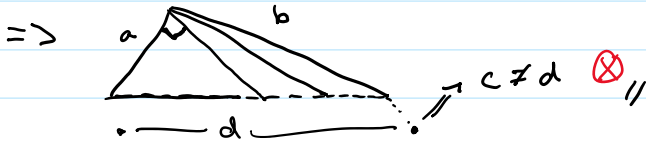
$$\begin{aligned} \text{area}(ABGF) &= 2 \text{area}(\triangle CBG) \\ \text{similarly, area}(ACHI) &= 2 \text{area}(\triangle BCI) \\ &= 2 \text{area}(\triangle ACD) \\ &= \text{area}(CDJK) \\ &= 2 \text{area}(\triangle ABE) \\ &= \text{area}(BEJK) \end{aligned}$$

Step 4: $\text{area}(ABGF) + \text{area}(ACHI)$
 $= \text{area}(BEJK) + \text{area}(CDJK)$
 $= \text{area}(BCDE)$

I-48) Converse of the pythagorean theorem



$a^2 + b^2 = c^2$
 \Rightarrow you have a right angle opposite
 suppose not, Build a right triangle
 with short sides a and b ...



$c^2 = a^2 + b^2 = d^2$ (by I-47)
 $\Rightarrow c = d$