Mathematics 2260H – Geometry I: Euclidean geometry

TRENT UNIVERSITY, Winter 2011

Quizzes

Quiz #1. Wednesday, 19 Thursday, 20 January, 2011 [10 minutes]

1. Given a line segment AB, construct a point C so that B is on AC and the length of AC is twice the length of AB. [5]

Quiz #2. Wednesday, 26 January, 2011 [10 minutes]

- 1. Suppose D is the midpoint of the side BC of $\triangle ABC$ and $\angle ADB = \angle ADC$. Show that AB = AC. [5]
- **Quiz** #2. Alternate version. [10 minutes]
- 1. Suppose D is the midpoint of the side BC of $\triangle ABC$ and AB = AC. Show that $\angle BAD = \angle CAD$. [5]

Quiz #3. Wednesday, 2 Thursday, 3 Monday, 7 February, 2011 [10 minutes]

1. Suppose that in $\triangle ABC$ and $\triangle DEF$, G and H are the midpoints of BC and EF, respectively, and that AG = DH and BG = EH. Use an example to show that the given triangles do not have to be congruent. [5]

Quiz #4. Wednesday, 9 February, 2011 [10 minutes]

1. Given a line segment AB, construct a quadrilateral with four equal sides, one of which is AB, and a right angle at A. [5]

Quiz #5. Wednesday, 16 Thursday, 17 February, 2011 [10 minutes]

1. Suppose line segments AB and CD each bisect the other at their intersection point E. Show that AC is parallel to BD. [5]

Quiz #6. Some day or other. [10 minutes]

1. Assuming that the sum of the interior angles of a triangle is equal to two right angles, show that the sum of the interior angles of a (convex!) pentagon is equal to six right angles. [5]

Quiz #7. Wednesday, 9 March, 2011. [10 minutes]

1. Suppose ABCD is a quadrilateral such that $\angle ABC$ and $\angle BCD$ are right angles. Show that the area of ABCD is equal to $\frac{1}{2}(AB + CD)BC$. [5]

Quiz #8. Wednesday, 16 March, 2011. [10 minutes]

1. Suppose D, E, and F are collinear points on the side AC, AB, and BC, respectively, of $\triangle ABC$, and AD = DC and AB = BE. Compute $\frac{CF}{FB}$. [5]

Quiz #9. Wednesday, 23 March, 2011. [12 minutes]

1. Suppose O is the orthocentre of $\triangle ABC$, *i.e.* the point where the three altitudes meet. Show that A is the orthocentre of $\triangle OBC$. [5]

Quiz #10. Wednesday, 30 March, 2011. [10 minutes]

1. Suppose that the orthocentre (where the three altitudes meet) and the incentre (where the three angle bisectors meet) of $\triangle ABC$ are the same point. Show that $\triangle ABC$ is equilateral. [5]

Quiz #11. Wednesday, 36 April, 2011. [10 minutes]

1. Suppose D is the circumcentre of $\triangle ABC$ and D is on the same side of BC as A. Show that $\angle BDC = 2 \angle BAC$. [5]