Mathematics 2200H – Mathematical Reasoning TRENT UNIVERSITY, Fall 2023

Assignment #4

\mathbf{Sets}

Due on Friday, 6 October.*

You should refer to the handout *The Zermelo-Fraenkel Axioms of Set Theory* for the statements of said axioms. The proofs you are asked to do should be done informally using these axioms, rather than be formal deductions in the first-order language of set theory developed in class. (That was done mainly to help illustrate how formal first-order logic works.) If you are a really serious mathochist, you may do so nevertheless, but rest assured that you will be punishing yourself...

- **1.** Prove that if x is a set, then $\{x\}$ is a set, *i.e.* there exists a set y whose sole element is x. [3]
- **2.** If x and y are sets, then (x, y), *i.e.* { { x }, { x, y } }, is a set. [3]
- **3.** If A and B are sets, then $A \times B$, *i.e.* $\{(a, b) \mid a \in A \text{ and } b \in B\}$, is a set. [4]

^{*} Please submit your solutions via Blackboard's Assignments module, preferably as a single pdf. If submission on Blackboard fails, please submit your solutions to the instructor on paper or via email to sbilaniuk@ trentu.ca as soon as you can.