Mathematics 2200H – Mathematical Reasoning TRENT UNIVERSITY, Fall 2020 Assignment #2² + 2¹ + 2⁰ Cancellation Due on Friday, 6 November.

- **1.** Show that $+_{\mathbb{Z}}$ satisfies the cancellation law for addition, *i.e.* for all $a, b, c \in \mathbb{Z}$, $a +_{\mathbb{Z}} c = b +_{\mathbb{Z}} c$ implies that a = b. [6]
- **2.** Show that $\cdot_{\mathbb{Z}}$ satisfies the cancellation law for multiplication, *i.e.* for all $a, b, c \in \mathbb{Z}$ with $c \neq 0_{\mathbb{Z}}, a \cdot_{\mathbb{Z}} c = b \cdot_{\mathbb{Z}} c$ implies that a = b. [4]

Hint: Having negatives makes 1 pretty easy. 2 is comparatively hard; it's worth remembering that if $[(s,t)]_{\sim} \neq 0_{\mathbb{Z}} = [(0,0)]_{\sim}$, then we must have $s \neq t$, so either s = t + S(k) or t = s + S(k) for some $k \in \mathbb{N}$.

Some Recommended Halloween Reading

The Ballad of the Black Fox Skin, by Robert W. Service A Tale of the Thirteenth Floor, by Ogden Nash

A Night in the Lonesome October, by Roger Zelazny