Mathematics 1350H – Linear algebra I: matrix algebra TRENT UNIVERSITY, Fall 2008

Assignment #3 Due on Friday, 17 October, 2008. Linear optimization

In this assignment we will deal with the solid whose faces are (parts of) the planes given by the equations x = 0, y = 0, z = 0, x = 10, y = 10, z = 10, x + y + z = 25, and 2x - y - z = -10. Another way to look at this solid is as the set of points with coordinates (x, y, z) which satisfy *all* of the following seven inequalities: $x \ge 0$, $y \ge 0$, $z \ge 0$, $x \le 10$, $y \le 10$, $z \le 10$, $x + y + z \le 25$, and $2x - y - z \ge -10$.

- 1. Find the coordinates of all of the vertices of this solid and make as accurate a sketch as you can of it. [6]
- 2. Find the maximum value of the function f(x, y, z) = 2x + 2y + z on this solid and determine at which point(s) of the solid this maximum occurs. [4]

Note: In this context the inequalities defining the solid are called *linear constraints*. Problems involving the optimization of a linear function subject to linear constraints arise often enough to be pretty important in the real world. If you're interested in the methods used to solve such problems, you might consider taking MATH-COIS 3350H – *Linear programming*; the only prerequisite is MATH 1350H.

JENNET ... Poor father. In the end he walked In Science like the densest night. And yet He was greatly gifted. When he was born he gave an algebraic Cry; at one glance measured the cubic content Of that ivory cone his mother's breast And multiplied his appetite by five. So he matured by a progression, gained Experience by correlation, expanded Into a marriage by contraction, and by Certain physical dynamics Formulated me. And on he went Still deeper into the calculating twilight Under the twinkling of five-pointed figures Till Truth became for him the sum of sums And Death the long division. My poor father. What years and powers he wasted. He thought he could change the matter of the world From the poles to the simultaneous equator By strange experiment and by describing Numerical parabolas.

From *The Lady's Not For Burning*, by Christopher Fry. (My favourite play! *Stefan*)