

## Mathematics 1110H – Calculus I: Limits, Derivatives, and Integrals

TRENT UNIVERSITY, Fall 2018

### Assignment #5

#### Maple Differentiates

*Due on Friday, 19 October.*

The focus of this assignment is to play a little with what *Maple* can do with taking and manipulating derivatives.

1. Use *Maple* to find all the points where the graph of  $p(x) = 5x^5 + 4x^4 + 3x^3 + 2x^2 + x$  has slope 0, without taking the derivative of  $p(x)$  by hand. [2]
2. Use *Maple* to help determine which of the points from **1** are maxima (peaks), minima (valleys), or neither of the graph of  $p(x)$ . [2]

A differential equation is an equation in which the derivative(s) of some unknown function(s) appear. The usual task is to find the unknown functions that satisfy the equation; this normally requires some additional information about specific values of the function(s) and/or the derivative(s) at specific points in order to fully pin down the unknowns.

Consider the differential equation  $\frac{dy}{dx} = e^{x+y}$ , with initial condition  $y(0) = 0$  (*i.e.* with  $y = 0$  when  $x = 0$ ). A solution to this differential equation with the given initial condition would be a function  $y = f(x)$  that satisfies both the equation, *i.e.* such that  $f'(x) = e^{x+f(x)}$ , and the given initial condition, *i.e.* such that  $f(0) = 0$ . **Maple** has ways of finding such solutions ...

3. Use **Maple** to find (all the) solution(s) of this differential equation with the given initial condition. Plot your solution(s) and figure out the(ir) domain and range. [3]
4. Use **Maple** to find (all the) solution(s) of this differential equation with the initial condition  $y(0) = 1$  instead. Plot your solution(s) and figure out the(ir) domain and range. [3]