

MATH 1101Y 2009 Quiz 4 (a)

Differentiate the function.

1. (1 pt)

$$f(x) = \frac{x^3 - 3x^2 + \sqrt{x}}{x}$$

Solution: Since

$$\begin{aligned} f(x) &= x^2 - 3x + x^{-\frac{1}{2}}, \\ f'(x) &= 2x - 3 + \left(-\frac{1}{2}\right)x^{-\frac{3}{2}}. \end{aligned}$$

□

2. (2 pts)

$$\frac{2 - \sin x}{x + \cos x}$$

Solution:

$$\left(\frac{2 - \sin x}{x + \cos x}\right)' = \frac{-\cos x(x + \cos x) - (2 - \sin x)(1 - \sin x)}{(x + \cos x)^2}.$$

□

3. (2 pts)

$$\sqrt{e^x + \tan(3x)}$$

Solution:

$$\left(\sqrt{e^x + \tan(3x)}\right)' = \frac{1}{2\sqrt{e^x + \tan(3x)}} (e^x + \sec^2(3x) \cdot 3).$$

□