

**Mathematics 3790H – Analysis I: Introduction to analysis**  
TRENT UNIVERSITY, Winter 2012

**Assignment #5**  
**Squeezing more out of the Integral Test**  
*Due on Thursday, 16 February, 2012.*

Recall that we showed that  $\sum_{n=1}^{\infty} \frac{1}{n}$  diverged by interpreting the series as a sum of areas and comparing it to the area under the graph of  $f(x) = \frac{1}{x}$ .

1. Use area-comparison arguments to show that  $\sum_{n=1}^{\infty} \frac{1}{1+n^2}$  converges to some number between  $\frac{\pi}{4}$  and  $\frac{\pi}{2}$ . [10]