

**Mathematics 3790H – Analysis I: Introduction to analysis**  
TRENT UNIVERSITY, Winter 2012

**Assignment #3**

*Due on Thursday, 2 February, 2012.*

1. Give an example of a sequence  $a_n$  which satisfies the condition

*For all  $\varepsilon > 0$  there is a  $N$  such that for all  $n \geq N$ ,  $|a_n - a_{n+1}| < \varepsilon$ .*

but which does *not* converge. [10]

HINT: Compare the given condition to the Cauchy Convergence Criterion for sequences (§2.12 in the text). They're *almost* the same ...